



# Intra-day Co-optimization of the Natural Gas and Electric Networks: the GECO Project

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# Motivation: reliable fuel supply to gas-fired power plants

## Gas-fired power generation is expanding:

- Fast to permit, fast to build
- Economic & environmental advantages
- Replacing retiring coal & nuclear

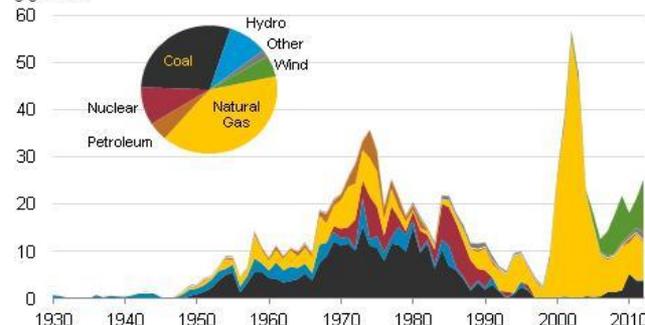
## Gas pipeline Loads are changing:

- Increasing in volume & variation
- More intermittent & uncertain

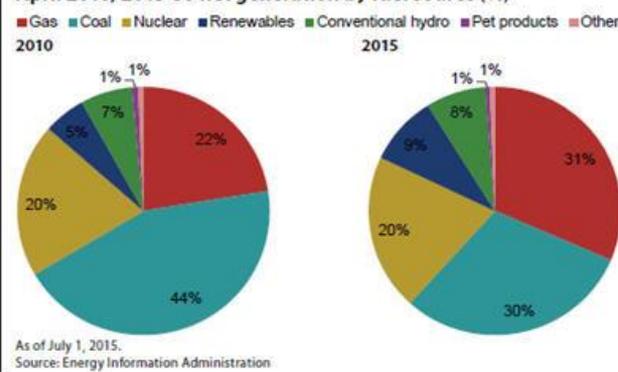
## Regulatory environment is evolving:

- FERC 787— need for information sharing
- FERC 809— market timing and coordination

Current (2012) capacity by initial year of operation and fuel type  
gigawatts



April 2010, 2015 US net generation by fuel source (%)



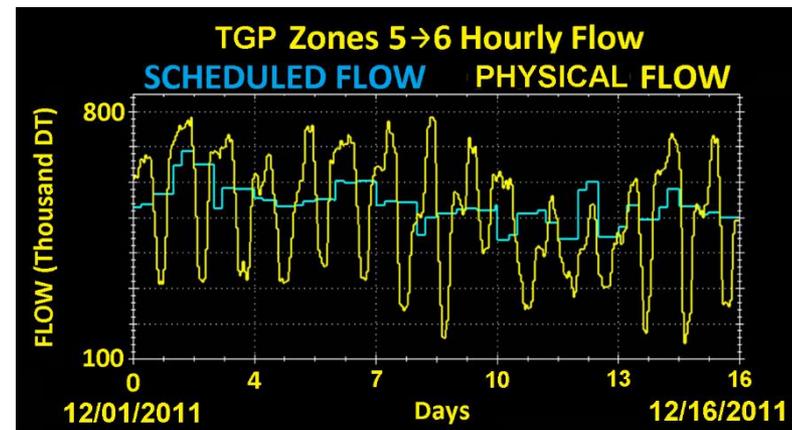
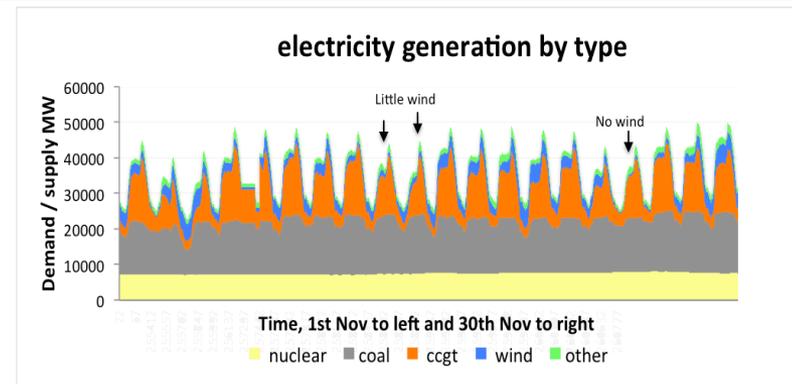
# Motivation: new challenges to intra-day gas pipeline operations

## Gas-fired generation fills power demand curve:

- Power plants activate and shut down daily
- Gas markets & flow schedules by static models cause mismatch of scheduled & observed flows

## Challenges to intra-day pipeline operations:

- **Variability:** intra-day dynamic flows that change daily with power-plant schedules
- **Coordination:** “burn sheets” & real-time information must be shared
- **Uncertainty:** power grid operations change quickly and unpredictably
- **Integration:** gas markets, flow scheduling, & physical operations done separately
- **Economics:** lack of meaningful economic signals exchanged between gas and power systems



# GECO Team

Institution	Expertise
Newton Energy Group & Consultants	Cloud platform for parallel modeling and analytics of energy systems. Data structures. Optimal pricing, market design, commercialization
Los Alamos National Laboratory	Advanced computational methods and algorithms for simulation and optimization of gas & electric networks
Polaris Systems Optimization	Advanced power systems simulator native to NEG cloud platform. Power systems optimization expertise
Boston University	Market design, market coordination, algorithms
AIMMS	Modeling language, optimization
Kinder Morgan	Pipeline operation, market expertise and information
PJM	Power system operation, market expertise and information

# Statement of Project Objectives

The objective of this project is to develop algorithmic structures and an associated market design that would enable a dramatically improved coordination and / or co-optimization of wholesale natural gas and electric physical systems and economic markets on a day-ahead and intra-day basis.

The key technology of the project will be:

- 1) novel methods, algorithms and software for simulation modeling and optimization of natural gas pipeline operation at the day-ahead and intra-day time scale;
- 2) a novel mechanism for pricing of natural gas delivered to end users and in particular to gas-fired power plants; and
- 3) novel mechanisms for coordinating natural gas and electric operations both day ahead and in real-time, based on locational prices of natural gas and electricity.

# Program Elements and Objectives

## Program Elements

### Software & Algorithms



- Software modules for pipeline simulations and optimization
- PSO SCUC/SCED with representation of pipeline constraints and decision cycles recognizing pipeline cycles and power system cycles
- Market model database, cloud infrastructure integrating PSO and pipeline modules and coordination modules

### Market Design



- Joint gas-electric theory of locational marginal prices (LMPs) and methods for computing gas LMPs
- Market design proposal including coordination mechanisms

### Realistic Market Simulations



- Gas-electric simulation model within the PJM footprint
- Set of simulated scenarios comparing performance of gas-electric coordination policies under different assumptions
- Results vetted with Kinder Morgan and PJM

# Approach

## Program Elements

### Software & Algorithms



- Will explicitly reflect dynamic simulations and dynamic optimization of pipeline operations subject to intra-day operational constraints;
- Interactions between natural gas flows in pipelines and the power flow;
- Periodically repeating decision cycles of generation bidding and deployment decisions and natural gas nomination decisions

### Market Design



- Development of the joint gas-electric theory of locational marginal prices (LMPs)
- Theoretical foundations for the provision of the access to pipeline capacity based on economic principles rather than on physical rights.
- Gas-electric coordination mechanisms combining the exchange of physical and locational price data between gas and electric
- The market design acceptable to market participants in both the gas and electric sector

### Realistic Market Simulations



- Will develop gas-electric simulation model within the PJM footprint; will use historical operational data to evaluate the feasibility of various possible market designs and to benchmark efficiency improvement achieved through coordination under each design relative to the status quo and/or to fully optimized joint system
- Will be based on the modeled representation of the PJM electrical system and pipelines serving their footprints.
- results reviewed and validated by PJM and by Kinder Morgan

# Project Objectives and Implications

Algorithmic Structures		Market Design
Co-optimization of physical systems		Coordination of gas and electric markets
	Current Technology	GECO Technology
<b>Pipeline operation control methods</b>	Primarily steady state modeling with "rule-based" compressor operations. Transient analysis performed in reliability context	Fast dynamic optimization of compressor operations incorporating transient effects
<b>Primary objectives of pipeline operation</b>	Maintaining security at least cost of compressor operations	Maintaining security at least cost of meeting system demand
<b>Price formation mechanisms</b>	Daily on weekdays only. Prices formed by traders at certain pipeline delivery points. Prices do not reflect intra-day pipeline operational constraints	Hourly 24/7 at each pipeline node. Prices formed by the optimization engine and are consistent with engineering and physics of pipeline operations
<b>Coordination</b>		
<b>Scheduling</b>	Daily quantity over a standard day. Intra-day profiling is opaque	Transparent intra-day scheduling
<b>Receipt and delivery points</b>	Rigid, based on priorities as specified in the shipping contract	Flexible, based on locational prices
<b>Delivery guarantee</b>	No guarantee for interruptible service customers	Economic mechanism to guarantee structured price/quantity delivery

# Gas pipeline optimization: status & why transients are a challenge

## Gas pipeline dynamics and control:

- Dynamics – **highly nonlinear, no simple model**
- Nominations – deliveries for next 12 to 24 hours
- Scheduling – compute flows to deliver nomination
- Control – real-time compressor adjustment

## Day-ahead market:

- Cleared daily to give nominations for flows
- Bilateral trading
- Ad-hoc, and capacity often based on static models

## Intra-day trading:

- Ad-hoc search for supply on spot market
- Simulation-informed manual tuning of flows

## • Gas pipeline physics:

(pressure, flow, line pack)  
**changes propagate slowly,**  
boundary flows always changing,  
**never stabilizes to steady-state**

## • Gas pipeline optimization:

(choosing compressor setpoints)  
Current methods use **steady-state models** – they work when there is low variation. **Very inaccurate given significant changes on an hourly basis**

# Gas Pipeline **Simulation**: meaning & state of the art

## Gas Pipeline **Simulation**: meaning & state of the art

### Simulation: an initial value problem (IVP)

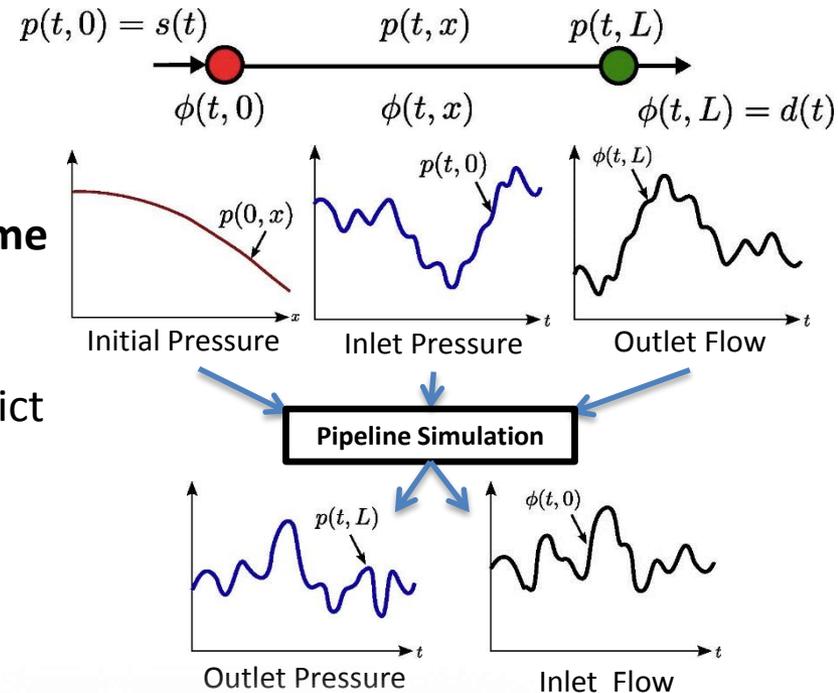
- State: instantaneous condition of system
- Parameters: initial state, boundary conditions
- **Start with initial state and evolve forward in time**

### Pipeline simulation:

- Given operating protocols of compressors, predict future flow & pressure based on physics
- At a space point, state is time-dependent trajectory (e.g. pressure as function of time)

### State of the art:

- Highly developed, sophisticated physics & engineering models, e.g., precise to < 1 psi



**PSIG** Pipeline Simulation Interest Group

# Gas Pipeline **Transient Optimization**: meaning & state of the art

## **Optimization: an optimal control problem (OCP)**

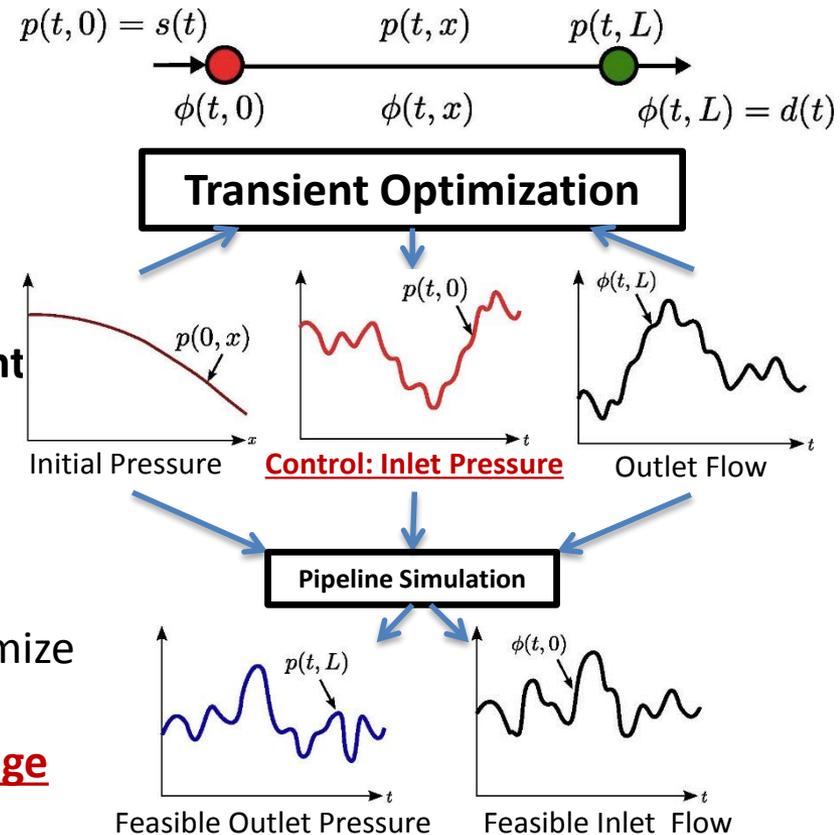
- State: instantaneous condition of system
- Parameters: initial state, boundary conditions
- Controls: parameters that can be chosen
- **Find controls & state as functions of time  $t \in [0, T]$  that satisfy feasibility & physics constraint while minimizing a cost objective**

## **Pipeline Optimization:**

- Given consumptions & pressure at a “slack” junction, compute compressor controls to minimize compressor power or maximize throughput

## **State of the art: long-standing and current challenge**

- **New tractable & scalable method from LANL**



# Continuous (PDE) Gas System Model to Reduced Network Flow

## Complete PDE model of gas pipeline network:

- Junctions  $j \in \mathcal{V} = \mathcal{V}_S \cup \mathcal{V}_D$  with given density  $s_j$  for  $j \in \mathcal{V}_S$  and given flux withdrawal (injection)  $d_j$  for  $j \in \mathcal{V}_D$
- Pipes  $\{i, j\} \in \mathcal{E}$  of length  $L_{ij}$ , diameter  $D_{ij}$ , and friction coefficient  $\lambda_{ij}$
- Flow  $\phi_{ij}(t, x_{ij})$  and density  $\rho_{ij}(t, x_{ij})$  with

$$\text{mass conservation: } \partial_t \rho_{ij} + \partial_x \phi_{ij} = 0$$

$$\text{momentum balance: } \partial_t \phi_{ij} + a^2 \partial_x \rho_{ij} = -\frac{\lambda}{2D} \frac{\phi_{ij} |\phi_{ij}|}{\rho_{ij}}$$

- Define nodal densities  $\rho_j(t)$  for  $j \in \mathcal{V}_D$
- Pressure continuity for  $\forall \{i, j\} \in \mathcal{E}$ :

$$\rho_{ij}(t, 0) = \alpha_{ij}(t) s_i(t), \quad \forall i \in \mathcal{V}_S,$$

$$\rho_{ij}(t, L_{ij}) = \alpha_{ji}(t) s_j(t), \quad \forall j \in \mathcal{V}_S,$$

$$\rho_{ij}(t, 0) = \alpha_{ij}(t) \rho_i(t), \quad \forall i \in \mathcal{V}_D,$$

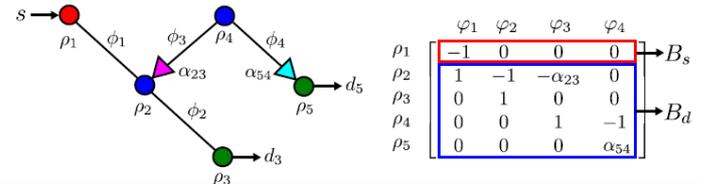
$$\rho_{ij}(t, L_{ij}) = \alpha_{ji}(t) \rho_j(t), \quad \forall j \in \mathcal{V}_D,$$

- Flow balance for  $\forall j \in \mathcal{V}_D$ :

$$d_j(t) = \sum_{i \in \mathcal{V}} \phi_{ij}(L_{ij}, t) - \sum_{k \in \mathcal{V}} \phi_{jk}(0, t)$$

Weighted incidence matrix  $B$  and incidence matrix  $A = \text{sign}(B)$

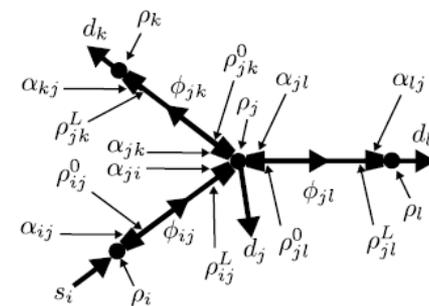
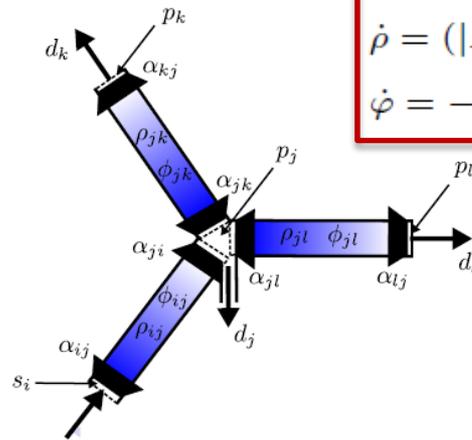
$$B_{ik} = \begin{cases} \alpha_{ij} & \text{edge } k = \pi_e(ji) \text{ enters node } i, \\ -\alpha_{ij} & \text{edge } k = \pi_e(ij) \text{ leaves node } i, \\ 0 & \text{else} \end{cases} \quad \text{where } \pi_e : \mathcal{E} \rightarrow \{1, \dots, |\mathcal{E}|\}$$



## Reduced Equations:

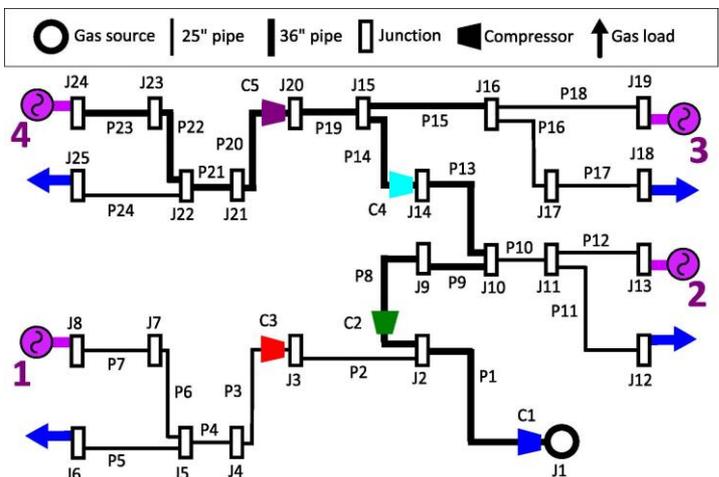
$$\dot{\rho} = (|A_d| \Lambda |B_d^T|)^{-1} [4(A_d \varphi - d) - |A_d| \Lambda |B_s^T| \dot{s}]$$

$$\dot{\varphi} = -\Lambda^{-1} (B_s^T s + B_d^T \rho) - K g(\varphi, |B_s^T| s + |B_d^T| \rho)$$



# Intra-day gas-grid interdependency case study

## Gas pipeline network model



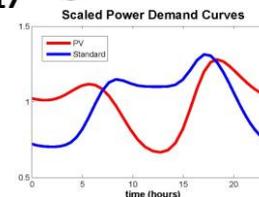
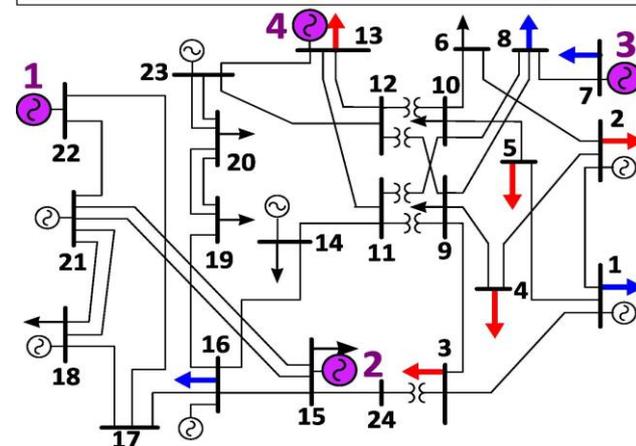
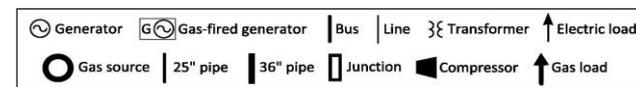
## Dynamic constraints on gas availability



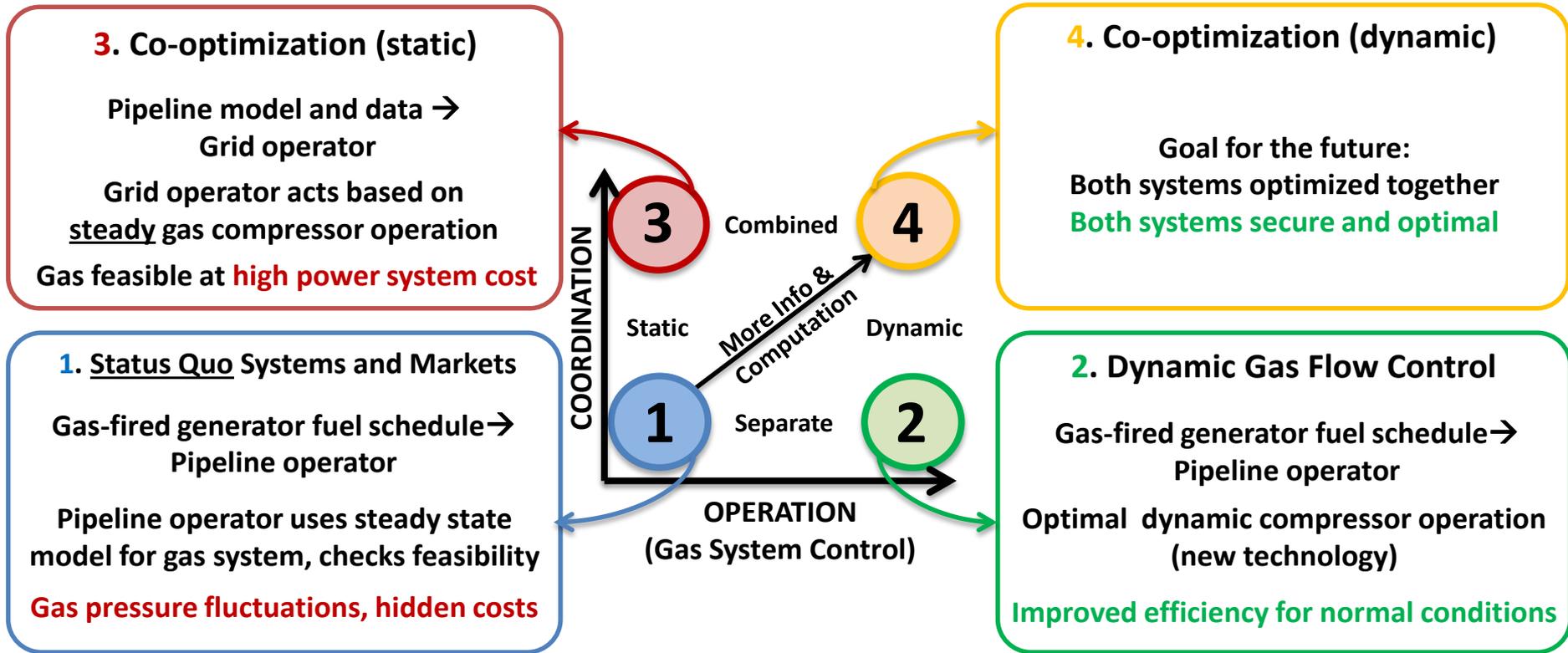
Simple model:  
Fixed gas price \$6/mmBTU,  
Quadratic heat rate curves,  
Quadratic generation cost curves

## Interdependency Simulation & Dynamic Gas-Grid Scheduling

## Power system model

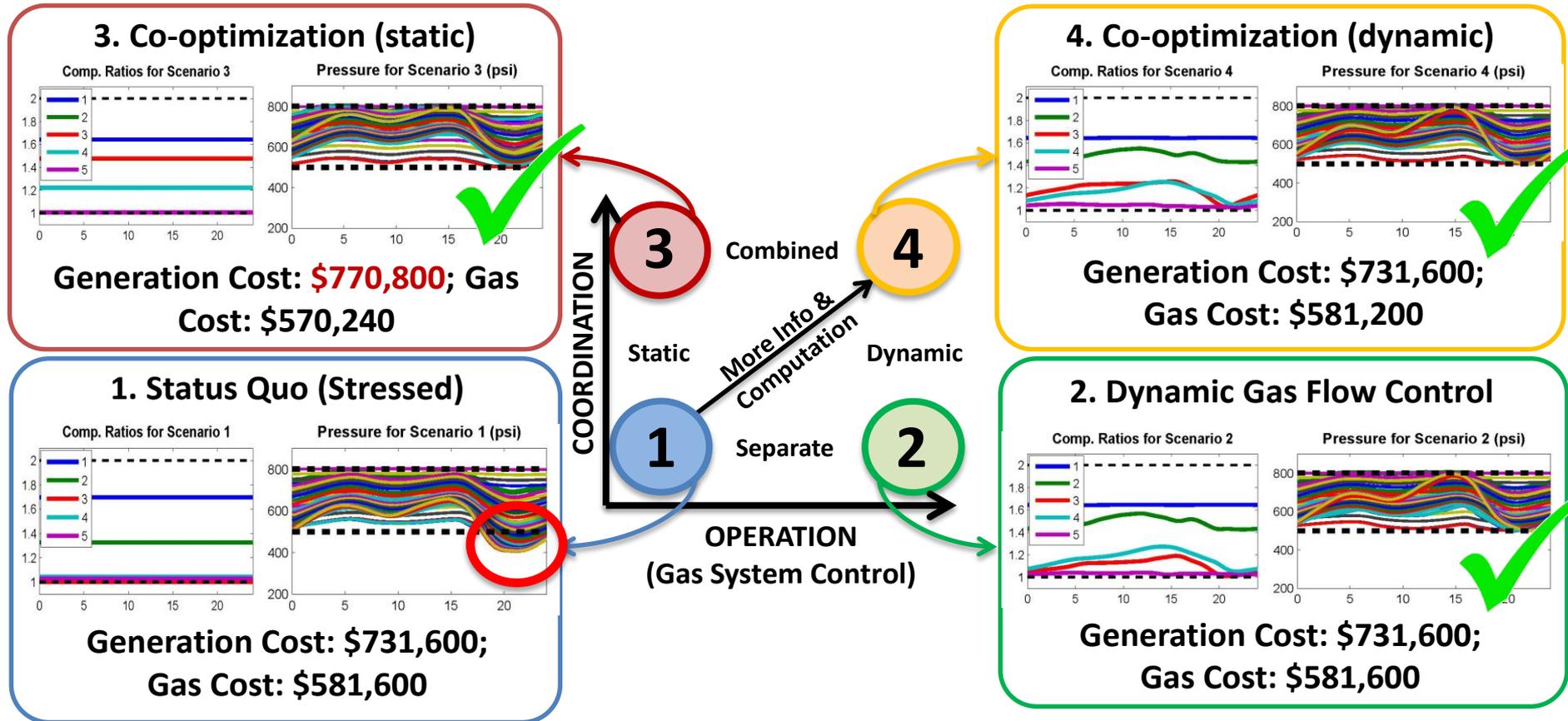


# Gas-grid coordination & co-optimization scenarios



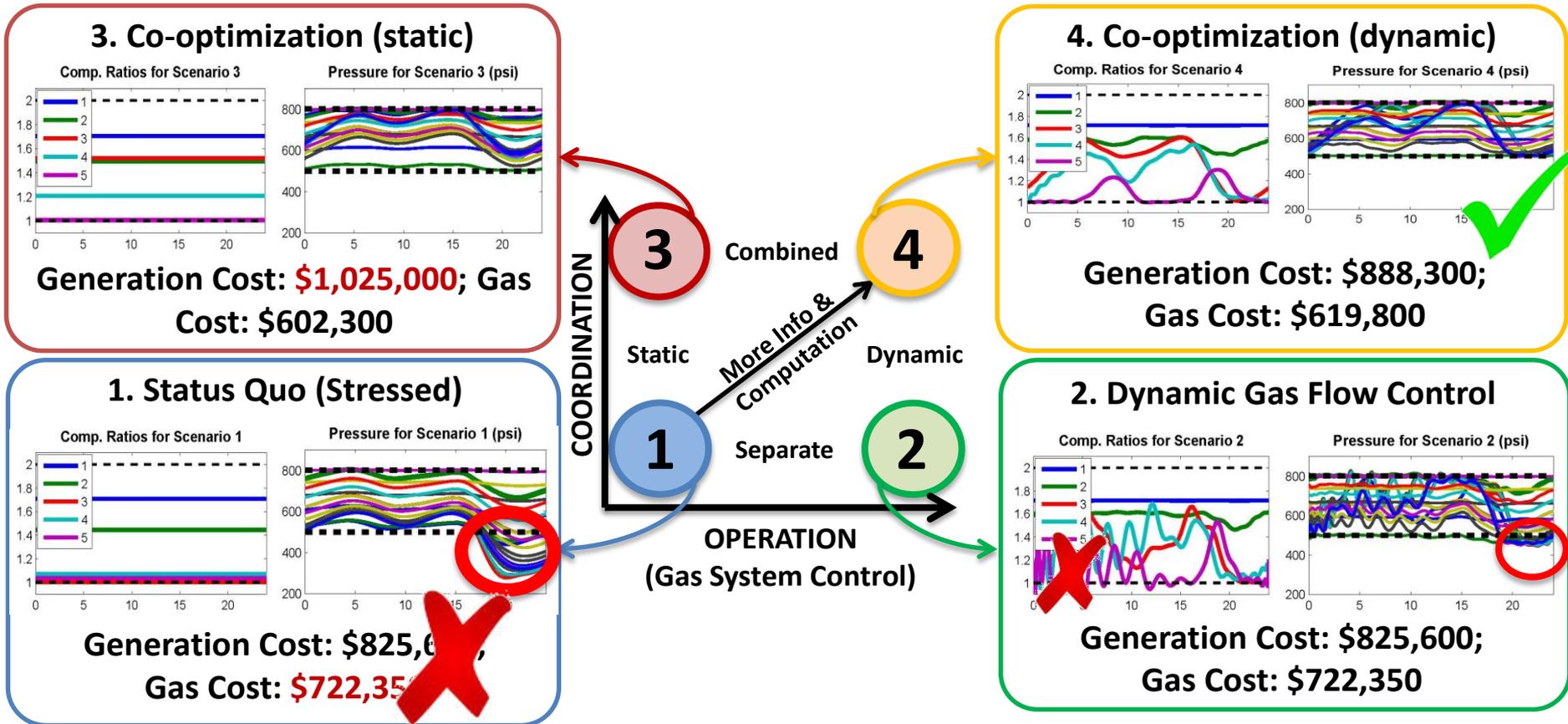
# Benefits of Coordination & Information Exchange

## Base Stress Case



# Benefits of Coordination & Information Exchange

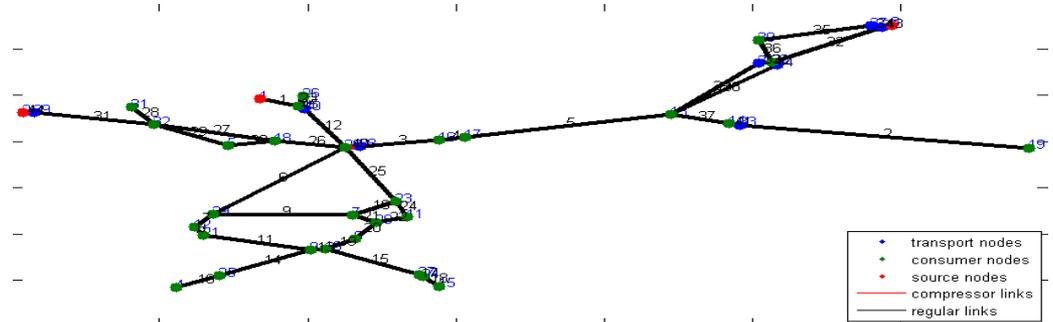
## High Stress Case



# “Gaslib40+” gas network case study

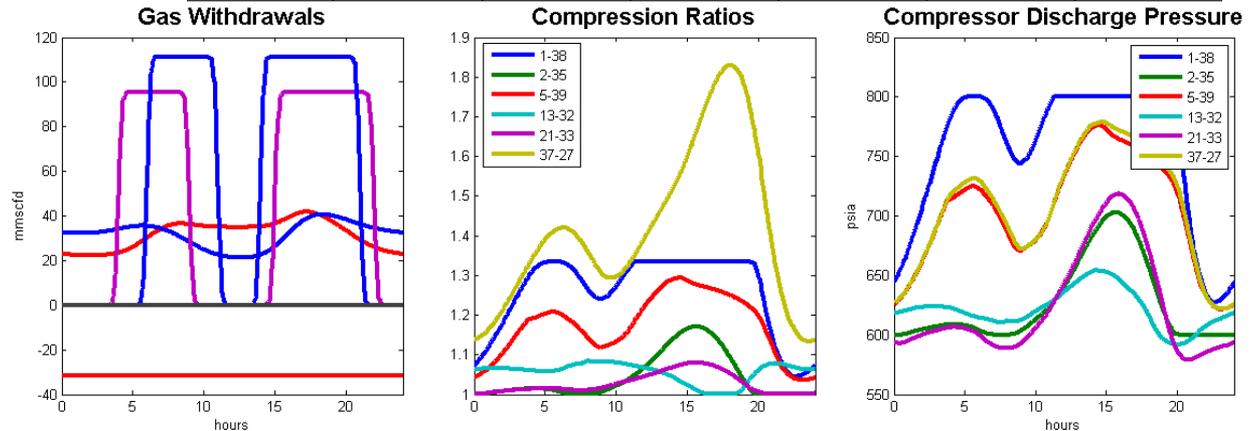
**Total system length: 2796km**

- Compressors: 6
- Supply points: 5
- Pressure nodes: 3
- Power plants: 7
- LDCs/other: 22



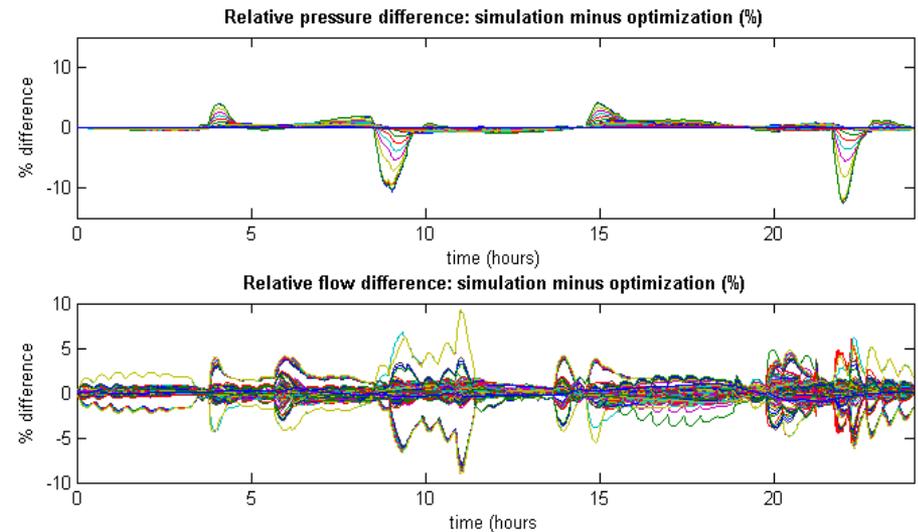
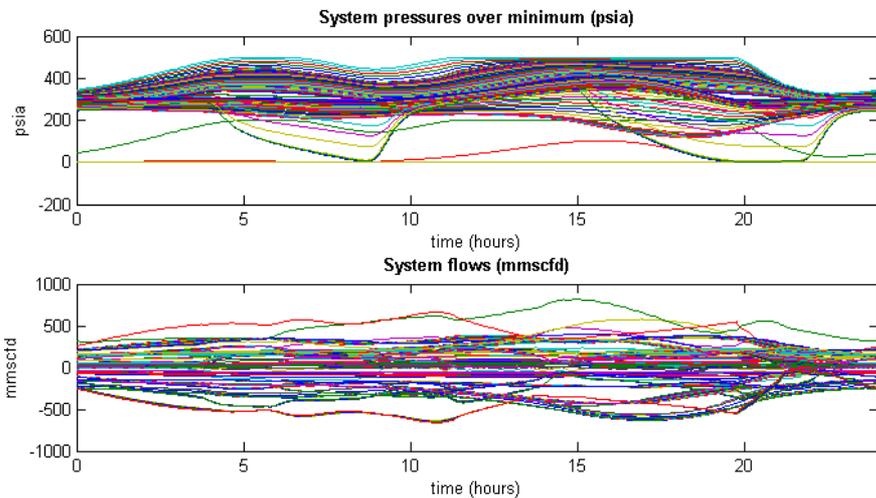
**Min. compressor power**

- 17.5km space disc
- 28min time disc
- Optimization time:  
256 sec
- Simulation time:  
5.88 sec (24h)



# “Gaslib40+” gas network case study

## Comparison of simulation and optimization results:



**Precision can be improved by finer discretization on better computing platform**



# A glimpse of gLMPs

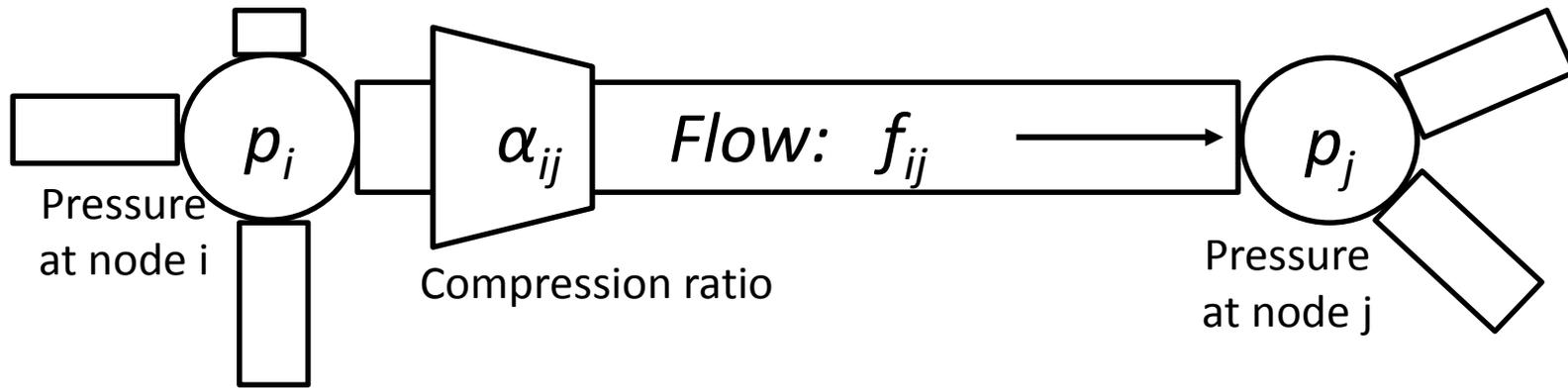
A steady state version

# General Gas Supply Optimization Formulation

- Considering a pipeline network
- Suppliers submit locational offers to sell gas into the pipeline system. These may include supplies received at interconnection points with other pipelines
- Off-takers submit locational bids to buy gas
- Maximize Social Welfare
  - = Sum {bid to buy times off-take volume}
  - Sum {offer to sell times supply volume}
  - Non-gas\*) compressor costs
- Dynamic optimization over one or several days

\*) Gas used for compression is accounted for explicitly through supplies

# Steady State Model



$$(\alpha_{ij} p_i)^2 - p_j^2 = \beta_{ij} f_{ij} |f_{ij}|$$

Steady state flow equation

$$\alpha_{ij} p_i \leq p^{\max}, p_j \geq p^{\min}$$

Pipe pressure limit constraints

$$E_{ij} = \eta_{ij} f_{ij} (\alpha_{ij}^{2m} - 1), E_{ij} \leq E_{ij}^{\max}$$

Compressor energy use and capacity constraint

$$\alpha_{ij} \geq 1$$

# Gas LMP Structure in the Steady State Model

$$LMP_j - LMP_i = \text{Compression}_{ij} + \text{Congestion}_{ij}^c + \text{Congestion}_{ij}^p$$

$$\text{Compression}_{ij} = LMP_i^* \eta_{ij} \left[ (\alpha_{ij}^{2m} - 1) + 2m\alpha_{ij}^{2m} \left( 1 - \frac{p_j^2}{\alpha_{ij}^2 p_i^2} \right) \right] - \theta_{ij} \frac{\beta_{ij} f_{ij}}{\alpha_{ij} p_i^2} \geq 0$$

$$\text{Congestion}_{ij}^c = \gamma_{ij} \eta_{ij} \left[ (\alpha_{ij}^{2m} - 1) + 2m\alpha_{ij}^{2m} \left( 1 - \frac{p_j^2}{\alpha_{ij}^2 p_i^2} \right) \right] \geq 0$$

$$\text{Congestion}_{ij}^p = \xi_{ij} \frac{\beta_{ij} f_{ij}}{\alpha_{ij} p_i} \geq 0$$

$LMP_i^*$  Gas or electric LMP depending on the compressor

$\theta_{ij}$  Dual variable for  $\alpha_{ij} \geq 1$

$\gamma_{ij}$  Dual variable for compressor capacity constraint

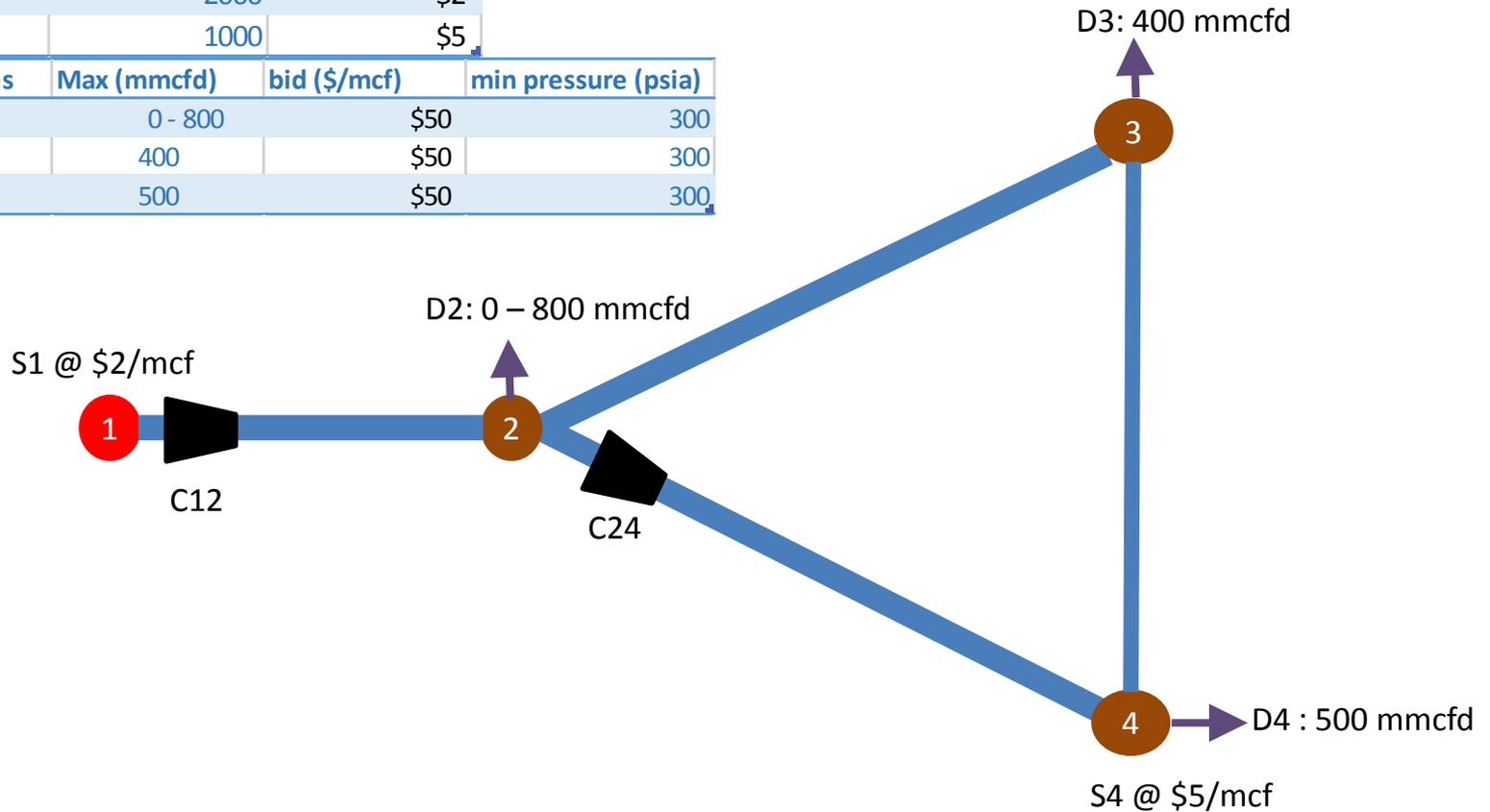
$\xi_{ij}$  Dual variable for pipe pressure constraint

# Numerical Example

Supply nodes	Max (mmcf/d)	price (\$/mcf)
1	2000	\$2
4	1000	\$5

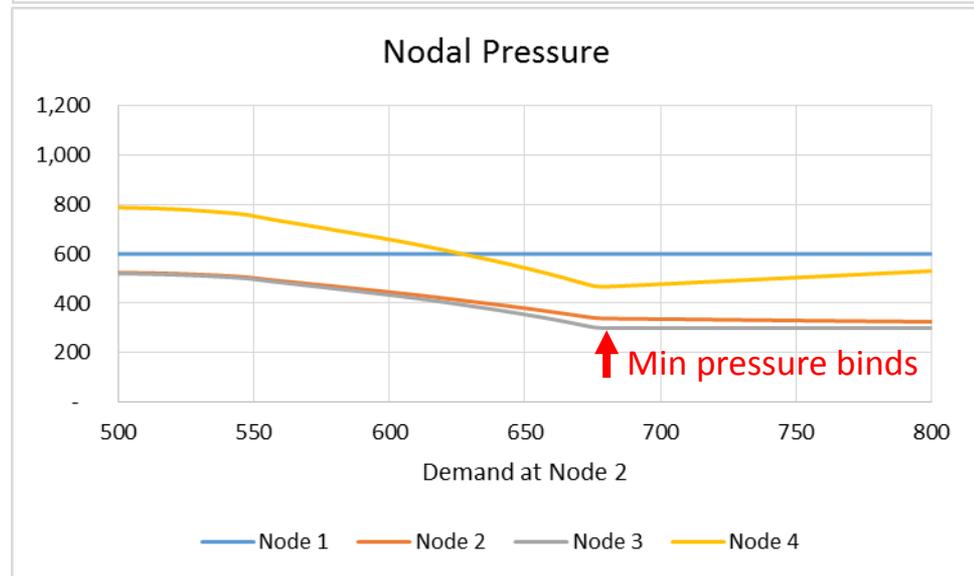
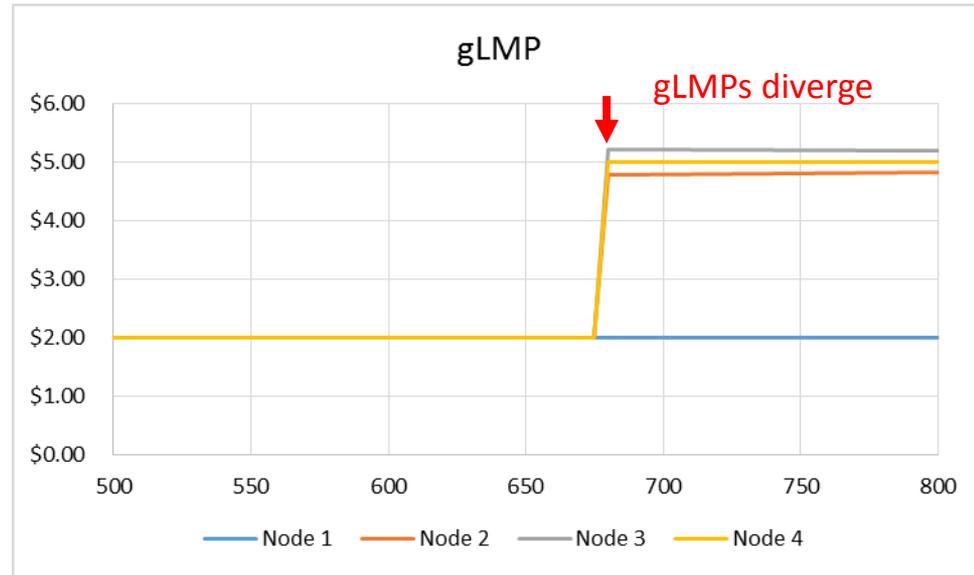
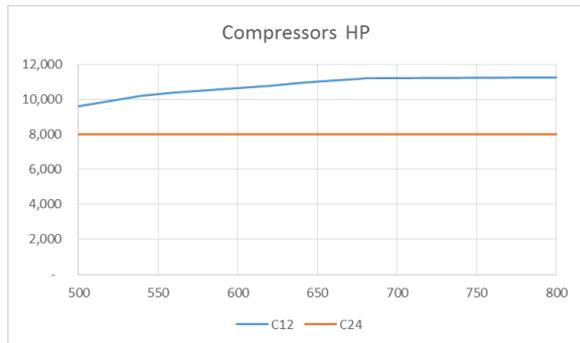
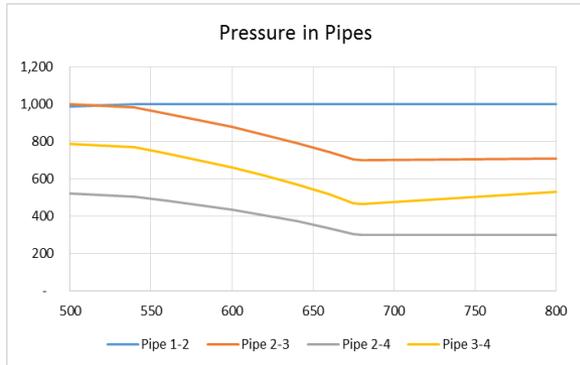
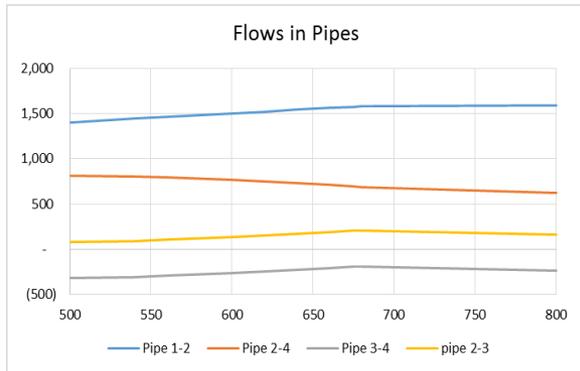
Demand nodes	Max (mmcf/d)	bid (\$/mcf)	min pressure (psia)
2	0 - 800	\$50	300
3	400	\$50	300
4	500	\$50	300



Pipes	length (miles)	diameter (in)	$\beta$	max pressure (psia)
1 - 2	50	36	0.35	1000
2 - 3	80	36	0.6	1000
2 - 4	80	36	0.6	1000
3 - 4	80	25	3.53	1000

Compressors	HP	$\eta$ (HP/mmcf/d)	m
12	12000	8.4	0.6
24	8000	8.4	0.6

# Optimal Solutions as a Function of Demand at Node 2



# Some Observations from gLMP Analysis

- Congestion does not necessarily translate into constrained pipe flows
  - Flow in pipe 1-2 continues to grow with demand at Node 2 despite pressure constraint
  - Flow in pipe 2-4 changes significantly while compressor C24 operates at maximum capacity
- In gas networks not every binding constraint triggers additional marginal resource
- Binding minimum pressure constraints may play major role in causing price separation

# Conclusions

- The opportunity exists to
  - radically change practical methods and algorithms of pipeline operations
  - Develop near real time pricing of natural gas that is consistent with the near real-time operations and with physics of the gas flow
- Realizing this opportunity is very important for gas and electric industry

# Information

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